

DISCUSSION:  
MONETARY POLICY AND HETEROGENEITY: AN  
ANALYTICAL FRAMEWORK  
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# MODELS OF CONSUMPTION

## Literature:

Enrich the **Consumption block** of the New Keynesian model

- Standard: Complete Markets (RANK models)

$$u'(c_t) = \beta(1 + r_{t+1})u'(c_{t+1})$$

- TANK models: Add Hand-to-mouth consumer

$$c_t = y_t.$$

- Heterogeneous Agent Incomplete markets

$$u'(c_t) = \beta(1 + r_{t+1})E_t u'(c_{t+1}).$$

# BILBIE: ANALYTICAL HANK

- Analytical HANK is a Stochastic TANK:
  - Unconstrained agents (S): Full access to credit markets.
  - Constrained agents (H) : Hand-to-mouth.
  - But with transition probabilities:
    - $S \rightarrow H$  with prob.  $1 - s$ .
    - $H \rightarrow S$  with prob.  $1 - h$ .

- Consumption:

$$\begin{aligned} \text{S type: } \quad u'(c_t^S) &= \beta(1 + r_{t+1})E_t u'(c_{t+1}) \\ &= \beta(1 + r_{t+1})[su'(c_{t+1}^S) + (1 - s)u'(c_{t+1}^H)] \end{aligned}$$

$$\text{H type: } \quad c_t^H = y_t^H$$

## BILBIE: ANALYTICAL HANK

- Linearizing Analytical HANK:

$$c_t = \delta E_t c_{t+1} - \sigma \frac{1 - \lambda}{1 - \lambda \chi} (i_t - E_t \pi_{t+1} - \rho_t),$$

where  $\delta \equiv 1 + (\chi - 1) \frac{1 - s}{1 - \lambda \chi},$

$$y_t^H = \chi Y_t,$$

$$\lambda = \frac{1 - s}{2 - s - h} \quad (\text{ss-mass of H-types}).$$

- For  $\chi = 1$ : Standard Euler Equation.

$$\begin{aligned} c_t &= 1 E_t c_{t+1} - \sigma \frac{1 - \lambda}{1 - \lambda} (i_t - E_t \pi_{t+1} - \rho_t), \\ &= E_t c_{t+1} - \sigma (i_t - E_t \pi_{t+1} - \rho_t) \end{aligned}$$

where  $\delta \equiv 1 + (\chi - 1) \frac{1 - s}{1 - \lambda \chi} = 1$

# INVESTMENT

- Resource constraint logic:  $Y = C + S = C + I$ .

$$C \uparrow \Rightarrow S \downarrow \Rightarrow I \downarrow$$

↪ Effect on Aggregate Demand  $C + I$  ???

- It matters for multipliers in  
Christiano, Eichenbaum & Rebelo (JPE, 2005).
- It matters for monetary policy transmission mechanism in  
Rupert & Sustek (On the Mechanics of NK Models).

↪ Value added:

Understand Inv. and interaction with MPC-hetero.

## FUNDAMENTAL AND POLICY $\chi$

- $\chi$  is considered a fundamental parameter.
- Seems right if  $Y$  is driven by fundamental shocks (technology, preferences, ...)

$\hookrightarrow \chi^{Fundamental}$

- BUT:  $\chi$  seems not to be policy-invariant.
- Two fiscal policies with same  $Y$  effect might have a very different distributional impact

$\hookrightarrow \chi^{Policy}$

## QUANTITATIVE IMPORTANCE OF $\chi$

- $\chi = 1$ : Complete Markets
- $\chi^{Policy}$  very different from 1  
(Hagedorn, Manovskii & Mitman: The Fiscal Multiplier).
  - Deficit financed govt' spending:  $\chi^{Policy} : 1.3 - 1.5$ .
  - Tax financed govt' spending:  $\chi^{Policy} : 0.6 - 0.7$ .
- $\chi^{Fundamental}$  close to 1 (e.g. Luetticke's JMP,...)
- Moving  $\chi^{Fundamental}$  requires hard work:
  - Find high MPC studies (Fagerang, Holm, Natvik for Norway), assume is all non-durable consumption ....
  - Large tailor-made redistribution
  - ...
- $\Rightarrow$  RANK  $\approx$  a-HANK  $\approx$  HANK

## WHAT MATTERS

Add **nominal bonds** to a-HANK or HANK. No further assumptions needed.

- **Reinterpretation of Friedman (63, 68, 79):**

*inflation is always and everywhere a monetary phenomenon . . .*

- **Fiscal determination of long-run inflation rate**, equal to the growth rate of nominal fiscal variables.
- **Price level determinate** for all specifications of monetary policy (no Taylor principle). Determined by monetary and fiscal policy.
- **Liquidity trap Puzzles disappear**
  - Divergence of fiscal multiplier at frictionless limit? NO
  - Contractionary TFP shocks expansionary? NO
  - Forward guidance infinitely powerful? NO (Hagedorn, Luo, Manovskii, Mitman)
- **Estimation:** See Kurt's talk tomorrow.



# CONCLUSION: A-HANK

Difference:

Nominal a-HANK  $\leftrightarrow$  RANK

**>**

Difference:

Real HANK  $\leftrightarrow$  Real a-HANK  $\leftrightarrow$  RANK